

## Math 8

Our Goal: To learn properties of exponents

Warm Up: Exponent review

Today's Homework

10.2 Exercises, p.420: 1-22

Previous Homework

10.1 Exercises, p.414: 1-20

$$\begin{aligned} 4^3 &= 4 \cdot 4 \cdot 4 \\ &= 16 \cdot 4 \\ &= 64 \end{aligned}$$

$$1^{50} = 1$$

$$0^5 = 0$$
$$= 0 \cdot 0 \cdot 0 \cdot 0 \cdot 0$$

Evaluate the expression.

1.  $3^5$

2.  $5^4$

3.  $10^6$

4.  $(-4)^3$

5.  $(-3)^2$

6.  $(-2)^5$

## Essential Question

How can you use inductive reasoning to observe patterns and write general rules involving properties of exponents?

**Work with a partner.**

a. Copy and complete the table.

Product	Repeated Multiplication Form	Power
$2^2 \cdot 2^4$		
$(-3)^2 \cdot (-3)^4$		
$7^3 \cdot 7^2$		
$5.1^1 \cdot 5.1^6$		
$(-4)^2 \cdot (-4)^2$		
$10^3 \cdot 10^5$		
$\left(\frac{1}{2}\right)^5 \cdot \left(\frac{1}{2}\right)^5$		

b. **INDUCTIVE REASONING** Describe the pattern in the table. Then write a *general rule* for multiplying two powers that have the same base.

$$a^m \cdot a^n = a^{\quad}$$

**Work with a partner. Write the expression as a single power. Then write a *general rule* for finding a power of a power.**

a.  $(3^2)^3 = (3 \cdot 3)(3 \cdot 3)(3 \cdot 3) = \quad$

b.  $(2^2)^4 = \quad$

c.  $(7^3)^2 = \quad$

d.  $(y^3)^3 = \quad$

e.  $(x^4)^2 = \quad$

Work with a partner. Write the expression as the product of two powers. Then write a *general rule* for finding a power of a product.

a.  $(2 \cdot 3)^3 = (2 \cdot 3)(2 \cdot 3)(2 \cdot 3) = \square \square \square \cdot \square \square \square$

b.  $(2 \cdot 5)^2 = \square$

c.  $(5 \cdot 4)^3 = \square$

d.  $(6a)^4 = \square$

e.  $(3x)^2 = \square$

Simplify the expression. Write your answer as a power.

1.  $2^4 \cdot 2^3$

$2^7$

2.  $7^5 \cdot 7^7$

3.  $\left(\frac{1}{2}\right)^2 \cdot \left(\frac{1}{2}\right)^5$

4.  $\left(-\frac{3}{5}\right)^3 \cdot \left(-\frac{3}{5}\right)^3$

5.  $x^5 \cdot x^{11}$

$x^5 \cdot x^{11}$   
 $5+11$   
 $x^{16}$

6.  $y^3 \cdot y$

$y^3 \cdot y^1$   
 $3+1$   
 $= y^4$

$$3^4 \cdot 3^{10} \neq 9^{14}$$

$$3^4 \cdot 3^{10} = 3^{14}$$

$$t^8 \cdot t^4 \cdot t^1$$

$$\begin{array}{c}
 \textcircled{4} + \textcircled{3} \\
 2 \cdot 2 \\
 (2 \cdot 2 \cdot 2 \cdot 2) \cdot (2 \cdot 2 \cdot 2) \\
 \textcircled{7} \\
 2
 \end{array}$$

## Key Ideas

### Product of Powers Property

**Words** To multiply powers with the same base, add their exponents.

**Numbers**  $4^2 \cdot 4^3 = 4^{2+3} = 4^5$       **Algebra**  $a^m \cdot a^n = a^{m+n}$

### Power of a Power Property

**Words** To find a power of a power, multiply the exponents.

**Numbers**  $(4^6)^3 = 4^{6 \cdot 3} = 4^{18}$       **Algebra**  $(a^m)^n = a^{mn}$

### Power of a Product Property

**Words** To find a power of a product, find the power of each factor and multiply.

**Numbers**  $(3 \cdot 2)^5 = 3^5 \cdot 2^5$       **Algebra**  $(ab)^m = a^m b^m$

a.  $2^4 \cdot 2^5$

b.  $-5 \cdot (-5)^6 =$

c.  $x^3 \cdot x^7 =$

$$\begin{aligned} (x^2)^3 &= x^2 \cdot x^2 \cdot x^2 \\ &\quad 2+2+2 \\ &= x^6 \\ &= x^6 \end{aligned}$$





**Simplify the expression.**

1.  $6^2 \cdot 6^4$       2.  $\left(-\frac{1}{2}\right)^3 \cdot \left(-\frac{1}{2}\right)^6$       3.  $z \cdot z^{12}$

4.  $(4^4)^3$       5.  $(y^2)^4$       6.  $((-4)^3)^2$

7.  $(5y)^4$       8.  $(ab)^5$       9.  $(0.5mn)^2$



A gigabyte (GB) of computer storage space is  $2^{30}$  bytes. The details of a computer are shown. How many bytes of total storage space does the computer have?

- (A)  $2^{34}$       (B)  $2^{36}$       (C)  $2^{180}$       (D)  $128^{30}$

**Exit Ticket:** Simplify.

$$5^3 \cdot 5^4$$

$$(-3x)^3$$