

Algebra 1

Our Goal: To learn to factor the difference of two squares

Warm Up: FOIL review

Today's Homework

- 7.7 Exercises, p.401: 4-40 (evens)
- iready is due tomorrow (the snow day did not make this a "short" week)

Previous Homework

7.6 Exercises, p.395: 4-32 (evens)

10) $8m^2 + 30m + 7$

Handwritten notes above the equation: $8m^2$, $4m$, $2m$

Handwritten factorizations below the equation:

$$\cancel{(8m + 7)(m + 1)}$$

$$(4m + 1)(2m + 7)$$

Simplify.

1. $(y-5)^2$

2. $(x+1)^2$

$$y^2 - 10y + 25 \quad x^2 + 2x + 1$$

3. $(3x-7)^2$

4. $(x-2y)^2$

$$9x^2 - 42x + 49$$

5. $(4x-9y)^2$

6. $(2x-7)^2$

Core Concept

Difference of Two Squares Pattern

Algebra

$$a^2 - b^2 = (a + b)(a - b)$$

Example

$$x^2 - 9 = x^2 - 3^2 = (x + 3)(x - 3)$$

Factor a. $x^2 - 25$

$$(x)^2 - (5)^2$$

$$(x+5)(x-5)$$

b. $4z^2 - 1$

$$(2z)^2 - (1)^2$$

$$(2z+1)(2z-1)$$

$$x^4 - 16$$

$$(x^2)^2 - (4)^2$$

$$(x^2+4)(x^2-4)$$

$$(x^2+4)(x+2)(x-2)$$

$a^2 + b^2$ is S.O.S. prime

$x^2 + 9$ is prime
 $\neq (x+3)(x+3)$

Use a special product pattern to evaluate the expression $54^2 - 46^2$.

Factor the polynomial.

$$\begin{array}{llll}
 1. x^2 - 36 & 2. 100 - m^2 & 3. 9n^2 - 16 & 4. 16h^2 - 49 \\
 (x+6)(x-6) & (10+m)(10-m) & (3n+4)(3n-4) & (4h+7)(4h-7)
 \end{array}$$

Use a special product pattern to evaluate the expression.

$$\begin{array}{llll}
 5. 36^2 - 34^2 & 6. 47^2 - 44^2 & 7. 55^2 - 50^2 & 8. 28^2 - 24^2
 \end{array}$$

Core Concept

Perfect Square Trinomial Pattern

Algebra

$$a^2 + 2ab + b^2 = (a + b)^2$$

$$a^2 - 2ab + b^2 = (a - b)^2$$

Example

$$\begin{aligned}
 x^2 + 6x + 9 &= x^2 + 2(x)(3) + 3^2 \\
 &= (x + 3)^2
 \end{aligned}$$

$$\begin{aligned}
 x^2 - 6x + 9 &= x^2 - 2(x)(3) + 3^2 \\
 &= (x - 3)^2
 \end{aligned}$$

Factor each polynomial.

a. $n^2 + 8n + 16$

$$(n)^2 \quad (4)^2$$

$$(n + 4)^2$$

b. $4x^2 - 12x + 9$

$$(2x)^2 \quad (3)^2$$

$$(2x - 3)^2$$

Solve $x^2 + \frac{2}{3}x + \frac{1}{9} = 0$.

$$(x)^2 \quad \left(\frac{1}{3}\right)^2$$

$$\left(x + \frac{1}{3}\right)^2 = 0$$

$$x = -\frac{1}{3}$$

Factor the polynomial.

9. $m^2 - 2m + 1$

$(m-1)^2$

10. $d^2 - 10d + 25$

$(d-5)^2$

$9(z^2 + 4z + 4)$

$9(z+2)^2$

11. $9z^2 + 36z + 36$

$9(z+2)^2$

Solve the equation.

12. $a^2 + 6a + 9 = 0$

$(a+3)^2 = 0$

$(a+3)^2 = 0$

$a = -3$

13. $w^2 - \frac{7}{3}w + \frac{49}{36} = 0$

$(w - \frac{7}{6})^2 = 0$

$(\frac{7}{6})^2 = 0$

14. $n^2 - 81 = 0$

$n^2 - 81 = 0$

$n = -9, 9$

A bird picks up a golf ball and drops it while flying. The function represents the height y (in feet) of the golf ball t seconds after it is dropped. The ball hits the top of a 32-foot-tall pine tree. After how many seconds does the ball hit the tree?



$y = 81 - 16t^2$

$$81 - 16t^2 = 32$$

$$32 \quad -32$$

$$49 - 16t^2 = 0$$

$$(\cancel{7+4t})(7-4t) = 0$$

$$7 - 4t = 0$$

$$t = \frac{7}{4} \text{ sec}$$

• **Exit Ticket:** Factor each polynomial.

a. $81 - x^2$

b. $x^2 - 24x + 144$

